

<b>6.1</b>	<b>Using Properties of Exponents</b>
<b>Objectives</b>	<p>1. Use properties of exponents to evaluate and simplify expressions involving powers.</p> <p>2. Use exponents and scientific notation to solve real life problems.</p>
	<p style="text-align: center;"><b>Properties of Exponents</b></p> <p>Product of Powers Property      <math>a^m \cdot a^n = \underline{\hspace{2cm}}</math></p> <p>Power of Power Property          <math>(a^m)^n = \underline{\hspace{2cm}}</math></p> <p>Power of a Product Property      <math>(ab)^m = \underline{\hspace{2cm}}</math></p> <p>Negative Exponent Property      <math>a^{-n} = \underline{\hspace{2cm}}</math></p> <p>Zero Exponent Property          <math>a^0 = \underline{\hspace{2cm}}</math></p> <p>Quotient of Powers Property      <math>\frac{a^m}{a^n} = \underline{\hspace{2cm}}</math></p> <p>Power of a Quotient Property      <math>\left(\frac{a}{b}\right)^m = \underline{\hspace{2cm}}</math></p>
<b>Evaluate. State which property you used.</b>	<p style="text-align: center;"> <math>\frac{7^6}{7^4}</math>    <math>3^{-2}</math>    <math>(3^2)^8</math> </p> <p style="text-align: center;"> <math>9^6(9^2)^{-3}</math>    <math>\left(\frac{3}{2^{-2}}\right)\left(\frac{1}{2}\right)^4</math> </p>

<p><b>Simplify the algebraic expression.</b></p>	$\left(\frac{x^{-3}}{y^2}\right)^4$ $yz^{-4}(x^2y)^3z$ $\frac{(c^4d)^2}{c^9d^2}$ $(-3a)^4a^9(-a^2)$ $-(4x^3)^{-2}$
	<p><b>Scientific Notation</b>  A number in the form <math>c \times 10^n</math> where, <math>1 \leq c &lt; 10</math> and <math>n</math> is an integer.</p>
<p><b>An average adult has about 528,000,000 feet of blood vessels in their body. How many times greater is this than the circumference of the Earth, which is about 25,000 miles?</b></p>	

<b>6.2</b>	<b>Evaluating and Graphing Polynomial Functions</b>																				
<b>Objectives</b>	<ol style="list-style-type: none"> <li>1. Evaluate a polynomial function.</li> <li>2. Graph a polynomial function.</li> </ol>																				
<b>Key Terms</b>	<p>Polynomial function</p> <p>Leading Coefficient</p> <p>Constant Term</p> <p>Degree</p>																				
<b>Standard Form of a Polynomial</b>	<table border="1" data-bbox="503 1018 1550 1344"> <thead> <tr> <th data-bbox="503 1018 771 1060">Degree</th> <th data-bbox="771 1018 1063 1060">Type</th> <th data-bbox="1063 1018 1550 1060">Standard Form</th> </tr> </thead> <tbody> <tr> <td data-bbox="503 1060 771 1123">0</td> <td data-bbox="771 1060 1063 1123"></td> <td data-bbox="1063 1060 1550 1123"></td> </tr> <tr> <td data-bbox="503 1123 771 1176">1</td> <td data-bbox="771 1123 1063 1176"></td> <td data-bbox="1063 1123 1550 1176"></td> </tr> <tr> <td data-bbox="503 1176 771 1228">2</td> <td data-bbox="771 1176 1063 1228"></td> <td data-bbox="1063 1176 1550 1228"></td> </tr> <tr> <td data-bbox="503 1228 771 1291">3</td> <td data-bbox="771 1228 1063 1291"></td> <td data-bbox="1063 1228 1550 1291"></td> </tr> <tr> <td data-bbox="503 1291 771 1344">4</td> <td data-bbox="771 1291 1063 1344"></td> <td data-bbox="1063 1291 1550 1344"></td> </tr> </tbody> </table>			Degree	Type	Standard Form	0			1			2			3			4		
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0																					
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<b>Decide whether the function is a polynomial. If it is, write the function in standard form and state its degree, type and leading coefficient.</b>	$f(x) = 2x^{1.2} + 2x^3 - 4x^2$ $f(x) = 0.32x - x^3 + 71$																				

## Synthetic Substitution

An alternate method for evaluation polynomials.

**Evaluate the function using direct substitution, then synthetic substitution.**

$$f(x) = 2x^4 - 4x^3 + x^2 + 3x - 1 \text{ when } x = 2$$

Direct

Synthetic

$$f(x) = 3x^5 - x^4 - 5x + 10 \text{ when } x = -2$$

Direct

Synthetic

$$f(x) = 3x^5 - 2x^2 + x \text{ when } x = 3$$

Direct

Synthetic

**End Behavior of a Polynomial Functions**

The graph of  $f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x^1 + a_0$

For  $a_n > 0$  and  $n$  even, \_\_\_\_\_ as  $x \rightarrow -\infty$

\_\_\_\_\_ as  $x \rightarrow +\infty$

For  $a_n > 0$  and  $n$  odd, \_\_\_\_\_ as  $x \rightarrow -\infty$

\_\_\_\_\_ as  $x \rightarrow +\infty$

For  $a_n < 0$  and  $n$  even, \_\_\_\_\_ as  $x \rightarrow -\infty$

\_\_\_\_\_ as  $x \rightarrow +\infty$

For  $a_n < 0$  and  $n$  odd, \_\_\_\_\_ as  $x \rightarrow -\infty$

\_\_\_\_\_ as  $x \rightarrow +\infty$

**Common Graphs**

$$f(x) = 3x$$

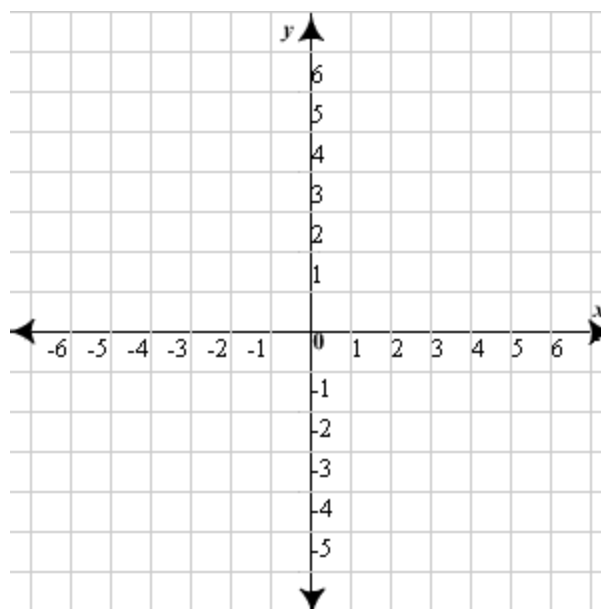
$$f(x) = -3x$$

$$f(x) = x^2$$

$$f(x) = -x^2$$

**Graph the function and describe the end behavior.**

$$f(x) = x^4 - 4x^2 + x$$



<b>6.3</b>	<b>Adding, Subtracting, and Multiplying Polynomials</b>
	<ol style="list-style-type: none"><li>1. Add, subtract, and multiply polynomials.</li><li>2. Use polynomial operations in real life problems.</li></ol>
<b>Addition and Subtraction of Polynomials</b>	<p>Add or subtract the coefficients of like terms (Do NOT change exponents.)</p> $(2x^3 - 4^2 + 5) + (-x^2 - 3x + 1)$ <p>Vertically</p> <p>Horizontally</p> $(x^2 + 1) - (3x^2 - 4x + 3)$ <p>Vertically</p> <p>Horizontally</p>

<b>Multiply the polynomials both vertically and horizontally.</b>	$(x + 2)(x^2 - x + 3)$ <p>Vertically</p> <p>Horizontally</p>
<b>Multiplying Three Polynomials</b>	$(x + 2)(x - 1)(x - 3)$ <p>Vertically</p> <p>Horizontally</p>
<b>Cube of a Binomial</b>	$(a + b)^3 = \underline{\hspace{10em}}$ $(x + 4)^3 = \underline{\hspace{10em}}$ $(a - b)^3 = \underline{\hspace{10em}}$ $(x - 5)^3 = \underline{\hspace{10em}}$
<b>Find the product.</b>	$(4x + 3)^3$



<b>6.4</b>	<b>Factoring and Solving Polynomial Equations</b>
	1. Factor polynomial expressions. 2. Use factoring to solve polynomial equations.
<b>Chapter 5 Factoring</b>	<b>General Trinomial</b>  <b>Perfect Square Trinomial</b>  <b>Difference of Two Squares</b>  <b>Common Monomial Factor</b>
<b>Special Factoring Patterns</b>	<b>Sum of Two Cubes</b> $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ Factor: $x^3 + 125$ $54y^4 + 16y$  <b>Difference of Two Cubes</b> $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$ Factor: $x^3 - 64$ $125x^3 - 27$

<p><b>Special Factoring Patterns</b></p>	<p><b>Factor by Grouping</b></p> <p>Factor: <math>4x^3 + 16x^2 + x + 4</math> <span style="float: right;"><math>x^3 - 3x^2 - 4x + 12</math></span></p> $x^2y^2 - 3x^2 - 4y^2 + 12$  <p><b>Factoring into Binomials</b></p> <p>Factor: <math>x^6 + 7x^3 + 10</math> <span style="float: right;"><math>25x^4 - 16</math></span></p> $4x^8 - 20x^6 + 24x^4$
<p><b>Solving Polynomial Equations</b></p>	<p><b>To solve a polynomial equation</b></p> <ol style="list-style-type: none"> <li>1. Set the equation equal to zero.</li> <li>2. Factor</li> <li>3. Set all factors equal to zero and solve.</li> </ol> <p>Solve: <math>2x^5 + 24x = 14x^3</math></p>

**Solving Polynomial Equations. Find the real number solutions of the equation.**

Solve:  $x^3 - 27 = 0$

$$x^3 + 2x^2 - 9x - 18 = 0$$

$$16x^8 = 81$$

**The revenue  $R$  in thousands of dollars for a small business can be modeled by  $R = t^3 - 8t^2 + t + 82$  Where  $t$  is the number of years since 1990. In which year did revenue reach \$90,000?**

<b>6.5</b>	<b>The Remainder and Factor Theorem</b>
<b>Objectives</b>	1. Divide polynomials and relate the result to the remainder theorem and factor theorem.
<b>Dividing Polynomials Using Long Division</b>	Divide: $(3x^5 - 2x^2 + 2x - 5) \div (x - 2)$
<b>The Remainder Theorem</b>	If a polynomial $f(x)$ is divided by $x - k$ , then the remainder is $r = f(k)$ .
<b>Divide Using Synthetic Division</b>	Divide: $(x^3 + x^2 - 5x + 3) \div (x + 2)$

	<p>Divide: <math>(2x^3 - x^2 + 3x + 4) \div (x + 1)</math></p> <p>Divide: <math>(x^4 - 16x^2 + x + 4) \div (x + 4)</math></p>
<p><b>The Factor Theorem</b></p>	<p>A polynomial <math>f(x)</math> has a factor <math>x - k</math> if and only if <math>f(k) = 0</math>.</p>
<p><b>Factor the polynomial, then find the other zeros of the function.</b></p>	<p>Factor the polynomial <math>f(x) = x^3 - 19x - 30</math> given that <math>f(5) = 0</math>, then find the other zeros of the function.</p> <p>Factor the polynomial <math>f(x) = 2x^3 - x^2 - 25x - 12</math> given that <math>f(4) = 0</math>, then find the other zeros of the function.</p>

<b>6.6</b>	<b>Finding Rational Zeros</b>
	<ol style="list-style-type: none"> <li>1. Find the rational zeroes of polynomial function.</li> <li>2. Use polynomial equations to solve real life problems.</li> </ol>
<b>Key Terms</b>	Rational Zeros
	$f(x) = 64x^3 + 12x^2 - 34x - 105$ <p style="text-align: center;">Zeros are <math>-\frac{3}{4}</math>, <math>-\frac{5}{4}</math>, and <math>\frac{7}{8}</math></p>
<b>Rational Zero Theorem</b>	<p>If <math>f(x) = a_nx^n + \dots + a_1x + a_0</math>, has integer coefficients, then every rational zero of the function has the following form:</p> $\frac{p}{q} = \frac{\text{factors of the constant term } a_0}{\text{factors of the leading coefficient } a_n}$
<b>Find the rational zeros of the function.</b>	$f(x) = x^3 + 5x^2 + 2x - 8$  $f(x) = x^3 - 4x^2 - 11x + 30$

**Find the rational zeros of the function.**

$$f(x) = 3x^3 + 12x^2 + 3x - 18$$

**Suppose you have 18 cubic inches of wax to make a candle in the shape of a pyramid with a square base. If you want the height to be 3 inches greater than the length of each side of the base, what should the dimensions of the candle be?**

Volume of a pyramid:  $V = \frac{1}{3}Bh$  B is the area of the base.