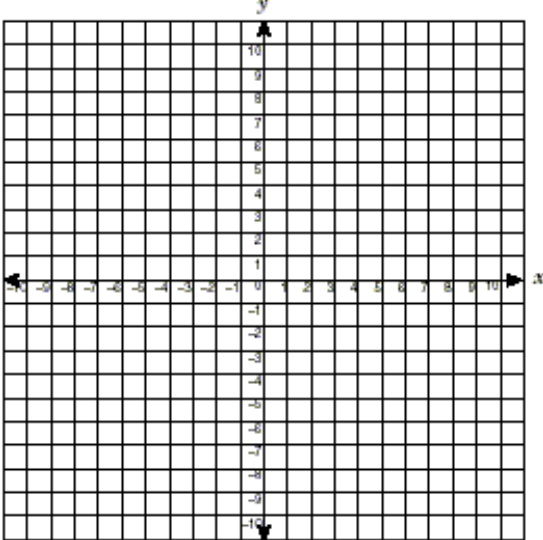


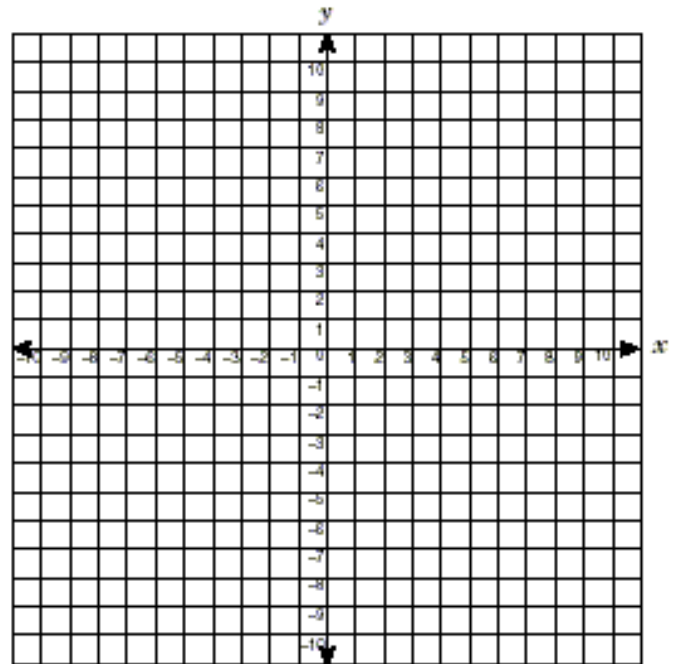
<b>8.1</b>	<b>Exponential Growth</b>
<b>Objective</b>	<ol style="list-style-type: none"> <li>1. Graph exponential growth functions.</li> <li>2. Use exponential growth functions to model real life situations.</li> </ol>
<b>Key Terms</b>	<p>Exponential Function</p> <p>Asymptote</p> <p>Exponential Growth Function</p>
<b>Basic Exponential Function</b>	<p><math>f(x) = 2^x</math></p> <div style="display: flex; align-items: center; justify-content: center;"> <div style="margin-right: 20px;"> <p>Y intercept _____</p> <p>Asymptote _____</p> <p>Domain _____</p> <p>Range _____</p> <p>End Behavior _____</p> <p>_____</p> </div>  </div>

**Graph the exponential functions.**

$$f(x) = \frac{1}{3} 2^x$$

$$f(x) = 3 \cdot 2^x$$

$$f(x) = -3 \cdot 2^x$$



Summary for  $f(x) = a \cdot 2^x$

End Behavior:

Asymptote:

y-intercept:

Domain:

Range:

## Exponential Growth Functions

$$y = a \cdot b^x$$

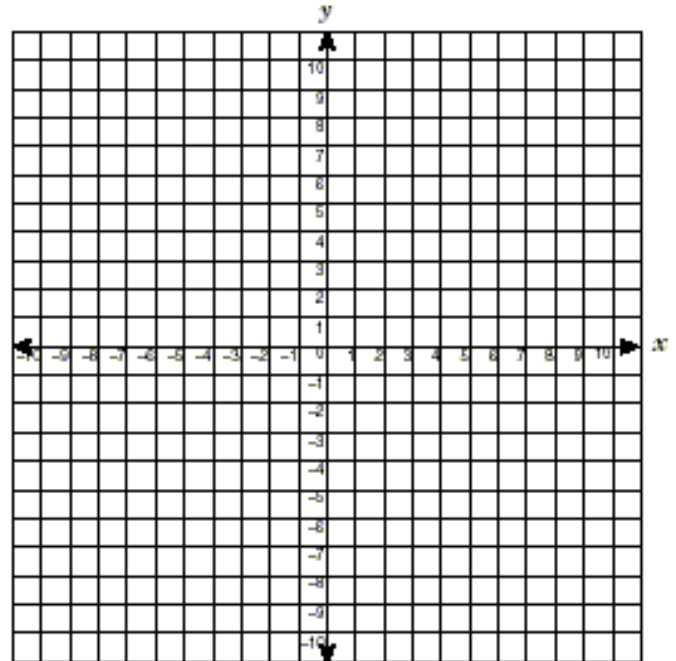
If  $a > 0$  and  $b > 1$

$$y = a \cdot b^{x-h} + k$$

$h$  moves the graph left and right.

$k$  moves the graph up and down.

Graph  $y = 2 \cdot 3^{x-1} - 3$



## Exponential Growth Model

$$y = a(1 + r)^t$$

$a$  is the initial amount

$r$  is the percent increase written as a decimal

$t$  is time period

$1 + r$  is the growth factor

In the last ten years an initial population of 44 deer grew by 8% per year, how many were in the park after 5 years?

### Compound Interest

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

*A is the amount n years*

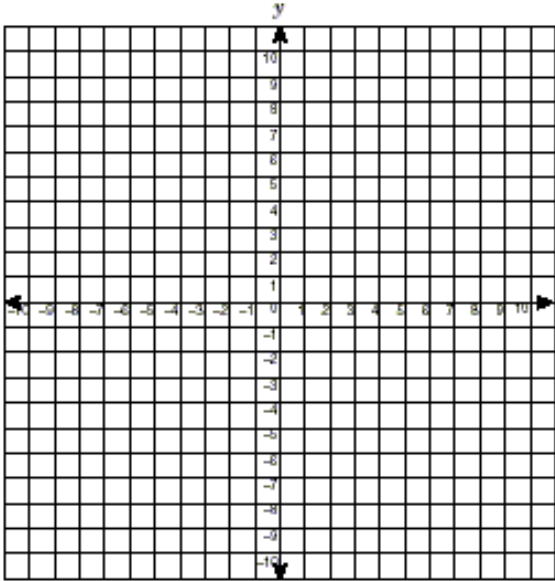
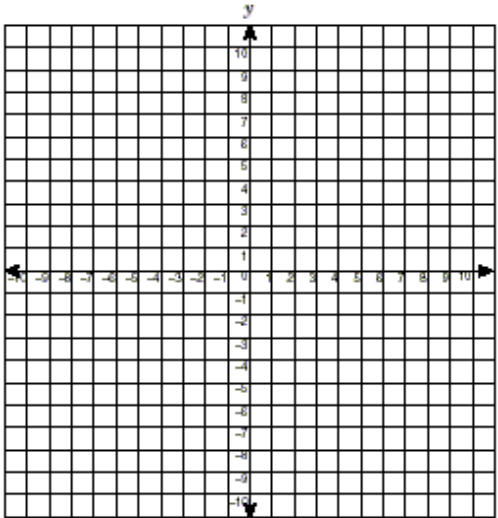
*P is the Principle  
initial amount*

*n is the number of times  
compounded per year*

*r is rate as a decimal*

*t is time in years*

**You deposit \$1400  
in an account that  
pays 4% annual  
interest. Find the  
balance after 2  
years. If the  
interest is  
compounded**  
a) Annually  
b) Quarterly  
c) Daily

8.2	<b>Exponential Decay</b>
<b>Objectives</b>	<ol style="list-style-type: none"> <li>1. Graph exponential decay functions.</li> <li>2. Use exponential decay functions to model real life situations.</li> </ol>
<b>Key Terms</b>	Exponential Decay Function
<b>Exponential Decay Functions</b> $y = a \cdot b^x$ <b>If <math>a &gt; 0</math> and <math>0 &lt; b &lt; 1</math></b>	<p>Graph <math>f(x) = 2\left(\frac{1}{3}\right)^x</math> State the domain and range.</p> 
<b>Exponential Decay Functions</b> $y = a \cdot b^{x-h} + k$ <b>If <math>a &gt; 0</math> and <math>0 &lt; b &lt; 1</math></b> <b><math>h</math> moves the graph left and right.</b> <b><math>k</math> moves the graph up and down.</b>	<p>Graph <math>f(x) = 5\left(\frac{1}{2}\right)^{x-3} + 4</math> State the domain and range.</p> 

### Exponential Decay Model

$$y = a(1 - r)^t$$

*a is the initial amount*

*r in the percent decrease  
written as a decimal*

*t is time period*

*1 - r is the decay factor*

**You purchase a car for \$20,000. The value of the car decreases by 15% each year. What is the value of the car after 5 years?**

**You have \$1000 and you lose half your money each day. How much money will you have after 10 days?**

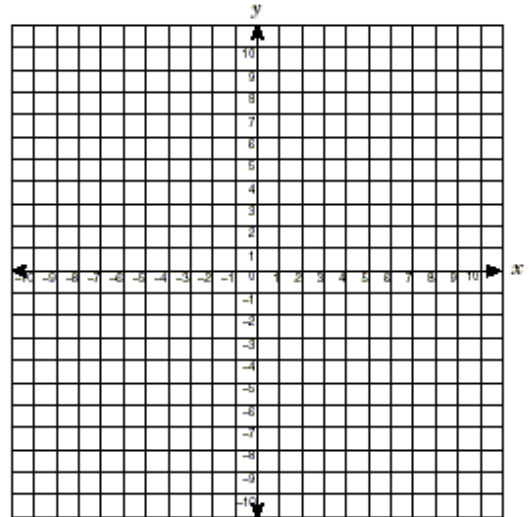
<b>8.3</b>	<b>The Number e</b>
<b>Objectives</b>	<ol style="list-style-type: none"> <li>1. Use the number e as a base of an exponential function.</li> <li>2. Use the natural base e in real life situations.</li> </ol>
<b>Key Terms</b>	Natural Base e
<b>Simplify the Natural Base Expression</b>	$e^6 e^8$ $\frac{6e^4}{2e^3}$ $(-4e^{3x})^2$ $\frac{12e^x}{e^{4x}}$ $\sqrt[3]{8e^{9x}}$
<b>Evaluate the Natural Base Expressions (Round Answers to Three Decimal Places)</b>	$e^3$ $e^{-3}$ $e^{0.7}$
<b>Tell whether the functions is an example of exponential growth or exponential decay</b>	$y = 5e^{-3x}$ $y = \frac{1}{4}e^{2x}$ $y = e^{-5x}$

**Graph the function.  
State the domain  
and range.**

$$y = e^{-2x}$$

Domain: \_\_\_\_\_

Range: \_\_\_\_\_



**Continuously Compounded Interest**

$$A = Pe^{rt}$$

*A = Amount after t years*

*P = Original Amount*

*r = interest rate (decimal)*

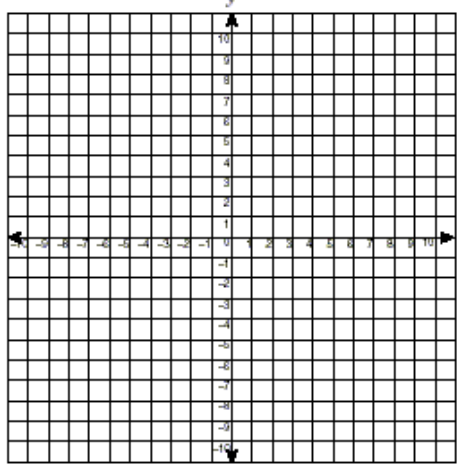
*t = time in years*

**Find the amount in  
an account after  
five years at 5.5%  
annual interest  
compounded  
continuously, if the  
original amount  
was \$2500.**

**Find the amount in  
the account if the  
interest was  
compounded  
quarterly.**



<b>8.4</b>	<b>Logarithmic Functions</b>																			
<b>Objectives</b>	1. Evaluate logarithmic functions.  2. Graph logarithmic functions.																			
	<p><b>Definition of a Logarithm with Base b</b>          Let b and y be positive numbers, <math>b \neq 1</math>.          The logarithm of y with base b is denoted by <math>\log_b y</math> and defined as follows:</p> $\log_b y = x \text{ if and only if } b^x = y$																			
	<p><b>Logarithmic Form</b>  <math>\log_b y = x</math></p> <p><b>Example:</b> <math>\log_3 81 = 4</math></p>	<p><b>Exponential Form</b>  <math>b^x = y</math></p> <p><math>3^4 = 81</math></p>																		
<b>Fill in the table.</b>	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th data-bbox="643 915 951 1003"><b>Logarithmic Form</b></th> <th data-bbox="951 915 1260 1003"><b>Exponential Form</b></th> </tr> </thead> <tbody> <tr> <td data-bbox="643 1003 951 1092"><math>\log_3 9 = 2</math></td> <td data-bbox="951 1003 1260 1092"></td> </tr> <tr> <td data-bbox="643 1092 951 1180"><math>\log_5 5 = 1</math></td> <td data-bbox="951 1092 1260 1180"></td> </tr> <tr> <td data-bbox="643 1180 951 1268"></td> <td data-bbox="951 1180 1260 1268"><math>2^3 = 8</math></td> </tr> <tr> <td data-bbox="643 1268 951 1356"></td> <td data-bbox="951 1268 1260 1356"><math>10^2 = 100</math></td> </tr> <tr> <td data-bbox="643 1356 951 1444"><math>\log_8 1 = 0</math></td> <td data-bbox="951 1356 1260 1444"></td> </tr> <tr> <td data-bbox="643 1444 951 1533"><math>\log_{\frac{1}{4}} 16 = -2</math></td> <td data-bbox="951 1444 1260 1533"></td> </tr> <tr> <td data-bbox="643 1533 951 1621"></td> <td data-bbox="951 1533 1260 1621"><math>5^{-2} = \frac{1}{25}</math></td> </tr> <tr> <td data-bbox="643 1621 951 1709"></td> <td data-bbox="951 1621 1260 1709"><math>\left(\frac{1}{3}\right)^{-2} = 9</math></td> </tr> </tbody> </table>		<b>Logarithmic Form</b>	<b>Exponential Form</b>	$\log_3 9 = 2$		$\log_5 5 = 1$			$2^3 = 8$		$10^2 = 100$	$\log_8 1 = 0$		$\log_{\frac{1}{4}} 16 = -2$			$5^{-2} = \frac{1}{25}$		$\left(\frac{1}{3}\right)^{-2} = 9$
<b>Logarithmic Form</b>	<b>Exponential Form</b>																			
$\log_3 9 = 2$																				
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$\log_{\frac{1}{4}} 16 = -2$																				
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	$\left(\frac{1}{3}\right)^{-2} = 9$																			

<b>Special Logarithm</b>	Let $b$ be a positive real number such that $b \neq 1$ .  <b>Logarithm of 1</b> $\log_b 1 = 0$ <i>because</i> $b^0 = 1$ <b>Logarithm of Base <math>b</math></b> $\log_b b = 1$ <i>because</i> $b^1 = b$			
<b>Evaluate the Expressions</b>	$\log_2 64$	$\log_5 125$	$\log_7 49$	
	$\log_{\frac{1}{2}} 0.25$	$\log_{\frac{1}{3}} 27$	$\log_{\frac{1}{4}} 256$	
	$\log_4 2$	$\log_{32} 2$	$\log_{81} 3$	
	<b>Common Logarithm</b> $\log_{10} x = \log x$		<b>Natural Logarithm</b> $\log_e x = \ln x$	
<b>Evaluate using your Calculator (Round answers to three decimal places)</b>	$\log 7$	$\log 150$	$\ln 0.5$	$\ln 40$
<b>Graphing Logarithmic Functions</b>	<b>Exponential and Logarithmic Functions are inverses of each other.</b>  Graph: $y = 3^x$ and $y = \log_3 x$			
				

By definition of a logarithm, the logarithmic function  
 $g(x) = \log_b x$  is the **inverse** of the exponential function  
 $f(x) = b^x$

**Find the inverse of the function.  
(Follow the process used in 7.4)**

$$y = \log_5 x$$

$$y = \ln x + 3$$

$$y = \log(x - 2)$$

$$y = \ln(x - 2)$$

$$y = \log_8 x - 4$$

$$y = \ln 3x$$



<p><b>Use <math>\log_3 4 \approx 1.262</math> and <math>\log_3 5 \approx 1.465</math> to approximate the value of the expression using the properties of logarithms.</b></p>	$\log_3 \frac{4}{5}$ $\log_3 20$ $\log_3 16$
<p><b>Expand the expression using the properties of logarithms.</b></p>	$\ln 22x$ $\log_5 2x^6$ $\log_6 \frac{6}{5}$ $\ln \frac{3y^4}{x^3}$
<p><b>Condense the expression using the properties of logarithms.</b></p>	$\ln 16 - \ln 4$ $\log_5 3 + 3\log_5 x - \log_5 4$ $2 \log x + \log 5$ $3(\ln 3 - \ln 3) + (\ln x - \ln 9)$

<p><b>Change of Base Formula</b></p>	<p>Let <math>u</math>, <math>b</math>, and <math>c</math> be positive numbers with <math>b \neq 1</math> and <math>c \neq 1</math>. Then:</p> $\log_c u = \frac{\log_b u}{\log_b c}$ <p>In particular <math>\log_c u = \frac{\log u}{\log c}</math> and <math>\log_c u = \frac{\ln u}{\ln c}</math></p>
<p><b>Evaluate using the change of base formula. Round answer to three decimal places.</b></p>	<p style="text-align: center;"> <math>\log_3 7</math>                      <math>\log_7 55</math>                      <math>\log_4 64</math> </p> <p style="text-align: center;"> <math>\log_{16} 4</math>                                      <math>\log_5 100</math> </p>
<p><b>The Richter magnitude <math>M</math> of an earthquake is based on the intensity <math>I</math> of the earthquake and the intensity <math>I_0</math> of an earthquake that can be barely felt.</b></p> $M = \log \frac{I}{I_0}$	<p>If the intensity of the 1994 LA earthquake was <math>10^{6.8}</math> times the <math>I_0</math>, what was the magnitude?</p> <p>If the intensity of an earthquake is 1000 times the <math>I_0</math>, what is the magnitude?</p>

<b>8.6</b>	<b>Solving Exponential and Logarithmic Equations</b>
<b>Objectives</b>	<ol style="list-style-type: none"> <li>1. Solve exponential equations.</li> <li>2. Solve logarithmic equations.</li> </ol>
	<p>If two powers with the same base are equal, then their exponents must be equal.</p> <p style="text-align: center;"><b>For <math>b &gt; 0</math> and <math>b \neq 1</math>, If <math>b^x = b^y</math>, then <math>x = y</math>.</b></p> <p>If two logarithms have the same base,</p> <p style="text-align: center;"><b>For positive numbers <math>b</math>, <math>x</math>, and <math>y</math> where <math>b \neq 1</math>, <math>\log_b x = \log_b y</math> if and only if <math>x = y</math>.</b></p>
<b>Solve the Equation.</b>	$2^{4x} = 32^{x-1} \qquad 27^{2x} = 9^{x+2} \qquad 4^{3x-2} = 16^x$ $4^x = 21 \qquad 5^x = 18 \qquad 7^x = 350$ $8 + 10^{5x+4} = 35 \qquad 3^{5x-2} - 4 = 3$

**Solve the Equation.**

$$\log_7(3x - 1) = \log_7(2x + 2)$$

$$\log_5(x + 6) = \log_5(3x - 4)$$

$$\log_3(2x + 3) = 4$$

$$16 \ln x = 30$$

$$\log 2x + \log(5x + 15) = 2$$

$$\ln x + \ln(x - 2) = 1$$

**You deposit \$5000 into an account that pays 6% annual interest compounded quarterly. How long will it take for the balance to reach \$10,000?**

**You have \$1,000,000. You lose half of it each day. How many days will it take until you have \$1?**



<b>8.7</b>	<b>Modeling with Exponential and Power Functions</b>
<b>Objectives</b>	<ol style="list-style-type: none"><li>1. Model data with exponential functions.</li><li>2. Model data with power functions.</li></ol>
	<b>Exponential Function</b> $y = ab^x$
<b>Write an exponential function <math>y = ab^x</math> whose graph passes through (1, 8) and (2, 32).</b>	
<b>Write an exponential function <math>y = ab^x</math> whose graph passes through (-1, 0.0625) and (3, 256).</b>	

**Power Function**

$$y = ax^b$$

**Write a power function  $y = ax^b$ , whose graph passes through (3, 4) and (6, 7).**

**Write a power function  $y = ax^b$ , whose graph passes through (4, 11) and (8, 14).**