

## Solving:

- Factorising
- Formula
- Completing the square
- Drawing a graph

**Factorising:**

easy...  $x^2 + 7x + 12 = 0$   
 $(x + 3)(x + 4) = 0$   
 $x = -3$  or  $x = -4$

brackets

... more difficult!

multiply

$3x^2 - 5x + 2$   
 $3x^2 - 3x - 2x + 2$   
 $3x(x - 1) - 2(x - 1)$   
 $(3x - 2)(x - 1)$

$\frac{b}{2 \times 3}$

## Quadratic Equations

$$ax^2 + bx + c$$

### The formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

### Completing the square:

$$x^2 + 4x - 3 = 0$$

half of 4x

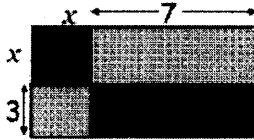
$$(x + 2)^2 - 4 - 3 = 0$$

$$(x + 2)^2 - 7 = 0$$

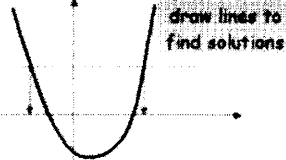
subtract 2<sup>2</sup>

$$x + 2 = \pm\sqrt{7}$$

$$x = \pm\sqrt{7} - 2$$



### Graphs:



Parabola - u shaped graph

### Difference of Two Squares:

$$x^2 - 16$$

$$(x - 4)(x + 4)$$

x squared subtract 4 squared

## Multi-Step Equations

**Solve each equation.**

1)  $-20 = -4x - 6x$

2)  $6 = 1 - 2n + 5$

3)  $8x - 2 = -9 + 7x$

4)  $a + 5 = -5a + 5$

5)  $4m - 4 = 4m$

6)  $p - 1 = 5p + 3p - 8$

7)  $5p - 14 = 8p + 4$

8)  $p - 4 = -9 + p$

9)  $-8 = -(x + 4)$

10)  $12 = -4(-6x - 3)$

11)  $14 = -(p - 8)$

12)  $-(7 - 4x) = 9$

13)  $-18 - 6k = 6(1 + 3k)$

14)  $5n + 34 = -2(1 - 7n)$

15)  $2(4x - 3) - 8 = 4 + 2x$

16)  $3n - 5 = -8(6 + 5n)$

17)  $-(1 + 7x) - 6(-7 - x) = 36$

18)  $-3(4x + 3) + 4(6x + 1) = 43$

19)  $24a - 22 = -4(1 - 6a)$

20)  $-5(1 - 5x) + 5(-8x - 2) = -4x - 8x$

**Solve by factoring.**

1.  $x^2 - 24x + 144 = 0$

2.  $x^2 - 20x + 100 = 0$

3.  $64x^2 + 16x + 1 = 0$

4.  $x^2 - 49 = 0$

5.  $x^2 + 6x - 55 = 0$

6.  $9x^2 - 49 = 0$

7.  $81x^2 - 1 = 0$

8.  $9x^2 + 24x + 16 = 0$

9.  $x^2 - 64 = 0$

10.  $x^2 - 5x - 84 = 0$

11.  $49x^2 - 168x + 144 = 0$

12.  $25x^2 - 60x + 36 = 0$

13.  $x^2 - x - 110 = 0$

14.  $x^2 - 16 = 0$

15.  $25x^2 - 36 = 0$

16.  $x^2 - 14x + 24 = 0$

17.  $49x^2 - 144 = 0$

18.  $x^2 + 7x + 10 = 0$

19.  $x^2 - 18x + 81 = 0$

20.  $25x^2 - 120x + 144 = 0$

21.  $49x^2 - 1 = 0$

22.  $25x^2 - 144 = 0$

23.  $x^2 + 2x + 1 = 0$

24.  $x^2 - 14x + 33 = 0$

25.  $x^2 - 81 = 0$

26.  $x^2 - 23x + 132 = 0$

27.  $x^2 - 144 = 0$

28.  $81x^2 - 100 = 0$

29.  $x^2 - 8x + 7 = 0$

30.  $36x^2 + 60x + 25 = 0$

## Rational Equations

Solve each equation. Remember to check for extraneous solutions.

1)  $\frac{1}{4x} - \frac{1}{4} = \frac{1}{2}$

2)  $\frac{5v-5}{v} - \frac{5v+15}{v} = 1$

3)  $\frac{5a+20}{6a} + \frac{1}{a} = \frac{3}{2a}$

4)  $\frac{2}{m^2} = \frac{1}{m} + \frac{1}{m^2}$

5)  $1 + \frac{4}{r-2} = \frac{5}{r-2}$

6)  $\frac{n-1}{2n} = 1 + \frac{1}{2n}$

7)  $\frac{5}{k} = \frac{1}{k} - 1$

8)  $\frac{5}{b} = \frac{1}{b} + 4$

## Square Root Equations

Solve each equation. Remember to check for extraneous solutions.

1)  $3 = \sqrt{b - 1}$

2)  $2 = \sqrt{\frac{x}{2}}$

3)  $\sqrt{-8 - 2a} = 0$

4)  $\sqrt{x + 4} = 0$

5)  $5 = \sqrt{r - 3}$

6)  $\sqrt{2m - 6} = \sqrt{3m - 14}$

7)  $\sqrt{8k} = k$

8)  $\sqrt{9 - b} = \sqrt{1 - 9b}$

9)  $\sqrt{3 - 2x} = \sqrt{1 - 3x}$

10)  $\sqrt{3k - 11} = \sqrt{5 - k}$

$$11) (20 - r)^{\frac{1}{2}} = r$$

$$12) (6b)^{\frac{1}{2}} = (8 - 2b)^{\frac{1}{2}}$$

$$13) \sqrt{56 - r} = r$$

$$14) \sqrt{-10 + 7p} = p$$

$$15) (18 - n)^{\frac{1}{2}} = \left(\frac{n}{8}\right)^{\frac{1}{2}}$$

$$16) \sqrt{2v - 7} = v - 3$$

$$17) -3 = (37 - 3n)^{\frac{1}{2}} - n$$

$$18) (-3 - 4x)^{\frac{1}{2}} - (-2 - 2x)^{\frac{1}{2}} = 1$$

$$19) x = 5 + (3x - 11)^{\frac{1}{2}}$$

$$20) 2 = \sqrt{3b - 2} - \sqrt{10 - b}$$